

Mae 20 Homework 4 solution

4-27 A copper-zinc alloy has the following properties:

grain diameter (mm)	strength (MPa)	$d^{-1/2}$
0.015	170 MPa	8.165
0.025	158 MPa	6.325
0.035	151 MPa	5.345
0.050	145 MPa	4.472

Determine (a) the constants in the Hall-Petch equation and (b) the grain size required to obtain a strength of 200 MPa.

Solution: The values of $d^{-1/2}$ are included in the table; the graph shows the relationship. We can determine K and σ_0 either from the graph or by using two of the data points.

$$\begin{aligned} \text{(a)} \quad 170 &= \sigma_0 + K(8.165) \\ 145 &= \sigma_0 + K(4.472) \\ \hline 25 &= 3.693K \end{aligned}$$

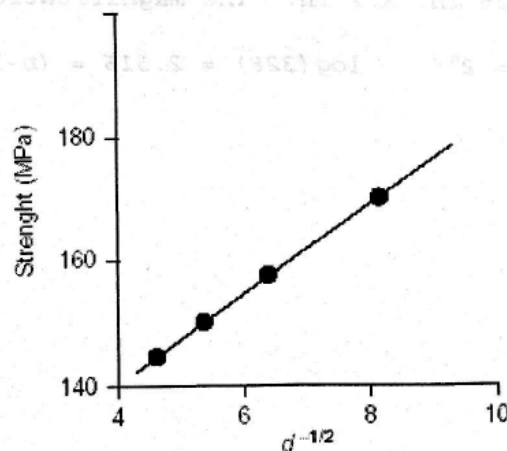
$$K = 6.77 \text{ MPa}/\sqrt{\text{mm}} \quad \sigma_0 = 114.7 \text{ MPa}$$

(b) To obtain a strength of 200 MPa:

$$200 = 114.7 + 6.77/\sqrt{d}$$

$$85.3 = 6.77/\sqrt{d}$$

$$d = 0.0063 \text{ mm}$$



- 4-31 Determine the ASTM grain size number for the materials in
 a. Figure 4-15 b. Figure 4-18

Solution: (a) There are about 26 grains in the photomicrograph, which has the dimensions 2.375 in. x 2 in. The magnification is 100, thus:

$$\frac{26}{(2.375)(2)} = 2^{n-1} \quad \log(5.47) = 0.738 = (n-1)\log(2) \quad n = 3.5$$

(b) There are about 59 grains in the photomicrograph, which has the dimensions 2.25 in. x 2 in. The magnification is 500, thus:

$$\frac{59(500/100)^2}{(2.25)(2)} = 2^{n-1} \quad \log(328) = 2.516 = (n-1)\log(2) \quad n = 9.4$$

4.33

The grain size of this 0.12% carbon steel is around 8.26×10^{-5} mm. As long as this material obeys the linear relationship of a Hall-Petch equation, we can use it to predict possible yield strength.

5-4 Atoms are found to move from one lattice position to another at the rate of 5×10^5 jumps per second at 400°C when the activation energy for their movement is 30,000 cal/mol. Calculate the jump rate at 750°C .

Solution: $\text{Rate} = \frac{5 \times 10^5}{x} = \frac{c_0 \exp[-30,000/(1.987)(673)]}{c_0 \exp[-30,000/(1.987)(1023)]}$
 $= \exp(-22.434 + 14.759)$

$$\frac{5 \times 10^5}{x} = \exp(-7.675) = 4.64 \times 10^{-4}$$

$$x = \frac{5 \times 10^5}{4.64 \times 10^{-4}} = 1.08 \times 10^9 \text{ jumps/s}$$

5.28

Solution: $D = 0.23 \exp[-32,900/(1.987)(1253)] = 42 \times 10^{-8} \text{ cm}^2/\text{s}$

$$\frac{1 - c_x}{1 - 0.1} = \text{erf}[x/(2\sqrt{(42 \times 10^{-8})(3600)})] = \text{erf}[x/0.0778]$$

$x = 0.01: \text{erf}[0.01/0.0778] = \text{erf}(0.1285) = \frac{(1 - c_x)}{0.9} = 0.144 \quad c_x = 0.87\% \text{ C}$

$x = 0.05: \text{erf}[0.05/0.0778] = \text{erf}(0.643) = \frac{(1 - c_x)}{0.9} = 0.636 \quad c_x = 0.43\% \text{ C}$

$x = 0.10: \text{erf}[0.10/0.0778] = \text{erf}(1.285) = \frac{(1 - c_x)}{0.9} = 0.914 \quad c_x = 0.18\% \text{ C}$

