

1.1

Problem Description:

A frictionless piston is raised slowly by heating the gas contained in the cylinder.

GIVEN:

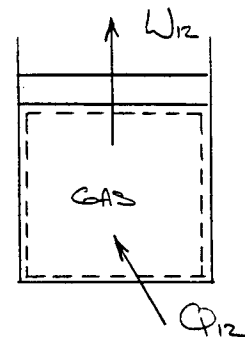
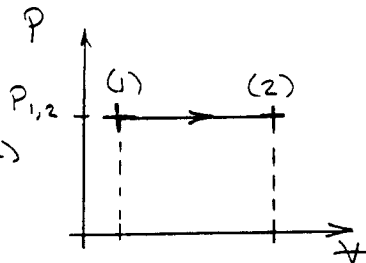
$$P_1 = 0.2 \text{ MPa}$$

$$P_2 = P_1 \text{ (constant pressure)}$$

$$V_1 = 1.0 \text{ m}^3$$

$$V_2 = 2.0 \text{ m}^3$$

$$Q_{12} = 2000 \text{ kJ} = 2 \text{ MJ}$$



DETERMINE: CHANGE IN INTERNAL ENERGY, ΔU_{12}

ENGINEERING MODEL:

- ① QUASIEQUILIBRIUM PROCESS
- ② SYSTEM IS THE GAS ONLY.
- ③ NEGLECTIBLE KINETIC AND POTENTIAL ENERGY EFFECTS.

BASIC EQUATIONS:

$$\text{1ST LAW FOR CLOSED SYSTEM: } Q_{\text{IN}} + W_{\text{IN}} = Q_{\text{OUT}} + W_{\text{OUT}} + \Delta KE + \Delta PE + \Delta U \quad (1)$$

$$\text{Work: } W_{12} = \int_1^2 p dV \quad (2)$$

STEPS:

Apply 1st law to system:

$$Q_{\text{IN},12} = W_{\text{OUT},12} + \cancel{\Delta KE} + \cancel{\Delta PE} + \Delta U_{12}$$

$$\text{SOLVING FOR } \Delta U_{12}: \quad \Delta U_{12} = Q_{\text{IN},12} - W_{\text{OUT},12} \quad (3)$$

To determine $W_{\text{OUT},12}$, use Eq. (2):

$$W_{\text{OUT},12} = |W_{12}| = \left| \int_1^2 p dV \right|$$

$$W_{\text{OUT},12} = |p(V_2 - V_1)| \quad (4)$$

SUBSTITUTING (4) INTO (3):

$$\Rightarrow \Delta U_{12} = U_2 - U_1 = Q_{\text{IN},12} - |p(V_2 - V_1)| \quad (5)$$

NUMERICAL SUBSTITUTION:

$$\text{Eq. (4)} \rightarrow W_{\text{OUT},12} = 0.2 \text{ MPa} (2. - 1.) \text{ m}^3 \left(\frac{1 \text{ N/m}^2}{1 \text{ Pa}} \right) \left(\frac{1 \text{ J}}{1 \text{ N}\cdot\text{m}} \right) = 0.2 \text{ MJ}$$

$$\text{Eq. (5)} \rightarrow \Delta U_{12} = 2 - 0.2 = \boxed{1.8 \text{ MJ}}$$