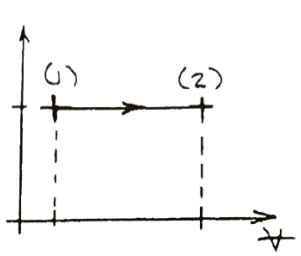
1.1

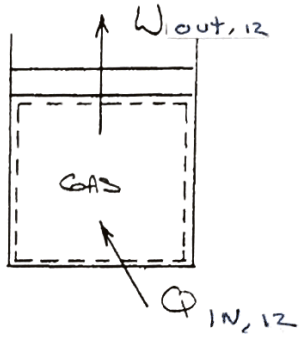
PROBLEM DESCRIPTION:

A FRICTIONLESS PISTON IS RAISED SLOWLY BY HEATING THE GAS CONTAINED IN THE CYLINDER.

GIVEN:

$p_1 = 0.2$ MPa
$p_2 = p_1$ (CONSTANT PRESSURE)
$\forall_1 = 1.0\ m^3$
$\forall_2 = 2.0\ m^3$
$Q_{12} = 2000$ kJ $= 2$ MJ





DETERMINE: CHANGE IN INTERNAL ENERGY, ΔU_{12}

ENGINEERING MODEL:
1. QUASIEQUILIBRIUM PROCESS
2. SYSTEM IS THE GAS ONLY.
3. NEGLIGIBLE KINETIC AND POTENTIAL ENERGY EFFECTS.

BASIC EQUATIONS:

1st LAW FOR CLOSED SYSTEM: $\Delta KE + \Delta PE + \Delta U = Q_{IN} + W_{IN} - Q_{OUT} - W_{OUT}$ (1)

WORK: $W_{12} = \int_1^2 p\,d\forall$ (2)

STEPS:

APPLY 1ST LAW TO SYSTEM:

$Q_{IN,12} = W_{OUT,12} + \cancel{\Delta KE}^{(3)} + \cancel{\Delta PE}^{(3)} + \Delta U_{12}$

SOLVING FOR ΔU_{12}: $\Delta U_{12} = Q_{IN,12} - W_{OUT,12}$ (3)

TO DETERMINE $W_{OUT,12}$, USE EQU. (2):

$W_{OUT,12} = |W_{12}| = \left| \int_1^2 p\,d\forall \right|$

$W_{OUT,12} = |p(\forall_2 - \forall_1)|$ (4)

SUBSTITUTING (4) INTO (3):

$\Rightarrow \Delta U_{12} = U_2 - U_1 = Q_{IN,12} - |p(\forall_2 - \forall_1)|$ (5)

NUMERICAL SUBSTITUTION:

EQU (4) $\rightarrow$ $W_{OUT,12} = 0.2\ MPa(2. - 1.)\ m^3 \left(\frac{1\ N/m^2}{1\ Pa}\right)\left(\frac{1\ J}{1\ N\,m}\right) = 0.2$ MJ

EQU (5) $\rightarrow$ $\Delta U_{12} = 2 - 0.2 = \boxed{1.8\ MJ}$