

Wind Tunnel Experiment

MAE 171A/175A

Objective:

Measure the Aerodynamic Forces and Moments of a Clark Y-14 Airfoil
Under Subsonic Flow Conditions

Measurement Techniques

- Pressure Distribution on Airfoil
- Drag from Momentum Loss Measured with a Wakefield Flow Array
- Direct Measurement with Mechanical Force

Procedure

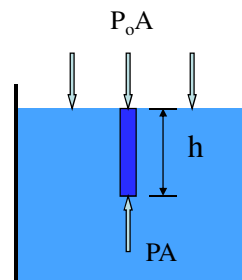
- Calibrate Tunnel w/ Pitot-Static Tube
- Measure Pressure Distribution on Airfoil
 - Different Flow Speeds & Angle-of-Attack
- Wakefield Measurement of Drag
- Mechanical Force Balance

Review of Hydrostatic Pressures

- Demonstration of pressure increase with depth
- Weight of the column $W=mg=\rho Ahg$
- Weight is supported by the net pressure $= (P - P_0)A$

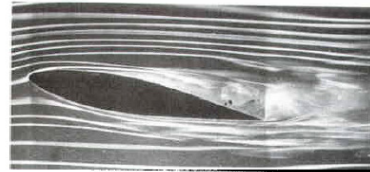
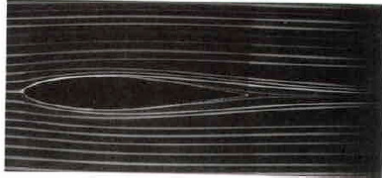
→ $P = P_0 + \rho hg$

- Pressure increases with depth
- All points at a given depth are at the same pressure



Review of fluid motion

- The motion of fluid depends on the Reynolds No.
 - Laminar
 - Turbulent



- The laminar flow may be presented by streamlines
- When the fluid velocity is large or when the fluid encounters most obstacles, the flow becomes turbulent

Describing Fluid Behavior at Isothermal Conditions

- Conservation of Mass
- Newtons Second Law of Motion

Conservation of Mass

$$\frac{\partial \rho}{\partial t} + \vec{\nabla} \cdot (\rho \vec{w}) = 0$$

ρ - density
 \vec{w} - velocity
 t - time

$$\vec{\nabla} = \vec{i} \frac{\partial}{\partial x} + \vec{j} \frac{\partial}{\partial y} + \vec{k} \frac{\partial}{\partial z}$$

Constant density:

$$\nabla \cdot \vec{w} = 0$$

Note: This is valid for unsteady flow

Newton's Second Law – Euler's Equation

$$\rho \frac{D\vec{w}}{Dt} = \rho \frac{\partial \vec{w}}{\partial t} + \rho (\vec{w} \cdot \vec{\nabla}) \vec{w} = -\vec{\nabla} p + \rho \vec{F}$$

p – pressure

\vec{F} - body force per unit mass

Assume body force is due to gravity, and it is conservative

$$\vec{F} = -g \vec{\nabla} z$$

g – acceleration due to gravity

Euler's Equation

Vector identity:

$$(\vec{w} \cdot \nabla) \vec{w} = \frac{1}{2} \vec{\nabla}(\vec{w} \cdot \vec{w}) - \vec{w} \times \nabla \times \vec{w}$$

Thus

$$\rho \frac{\partial \vec{w}}{\partial t} + \frac{1}{2} \rho \nabla(\vec{w} \cdot \vec{w}) + \nabla p + \rho g \vec{\nabla} z = \rho \vec{w} \times \nabla \times \vec{w}$$

Constant density

$$\frac{\partial \vec{w}}{\partial t} + \nabla \left[\frac{1}{2} \vec{w} \cdot \vec{w} + \frac{p}{\rho} + gz \right] = \vec{w} \times \nabla \times \vec{w}$$

Bernoulli's Equation – Steady Rotational Flow

Consider Flow Along a Streamline

$$\left\{ \vec{\nabla} \left[\frac{1}{2} \vec{w} \cdot \vec{w} + \frac{p}{\rho} + gz \right] - \vec{w} \times \vec{\nabla} \times \vec{w} \right\} \cdot d\vec{S}$$

Along a streamline

$$\frac{1}{2} \vec{w} \cdot \vec{w} + \frac{p}{\rho} + gz = \text{const}$$

Bernoulli Equation – Unsteady Irrotational Flow

$$\nabla \times \vec{w} = 0 \quad \vec{w} = \vec{\nabla} \phi$$

$$\nabla \left[\frac{\partial \phi}{\partial t} + \frac{1}{2} \vec{w} \cdot \vec{w} + \frac{p}{\rho} + gz \right] = \vec{w} \times \vec{\nabla} \times \vec{w} = 0$$

$$\frac{\partial \phi}{\partial t} + \frac{1}{2} \vec{w} \cdot \vec{w} + \frac{p}{\rho} + gz = \text{const}$$

Applications of Bernoulli's Equation

- We Measure Flow Velocity Using Bernoulli's Eqn:

$$P_a + \frac{1}{2} \rho_a U_a^2 = P_b + \frac{1}{2} \rho_b U_b^2$$

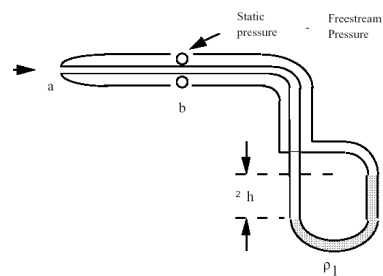
where:

$$U_a = 0, U_b = U_\infty$$

$$P_a - P_b = \frac{1}{2} \rho_\infty U_\infty^2 = q_\infty \quad \text{or} \quad P_a - P_b = \rho_1 \cdot \Delta h \cdot g$$

and:

$$U_\infty = \left(\frac{2(P_a - P_b)}{\rho_\infty} \right)^{1/2} \quad \text{or} \quad U_\infty = \left(\frac{2\rho_1 \Delta h g}{\rho_\infty} \right)^{1/2}$$

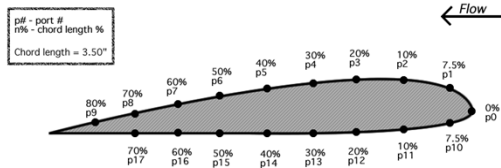


Pitot Probe: Measurement of Fluid Velocity

Δh is determined experimentally

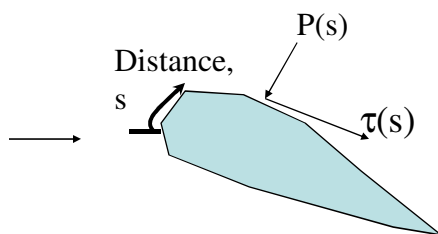
Pitot tube was invented by a Frenchman Henry Pitot in 1732

Pressure Distribution



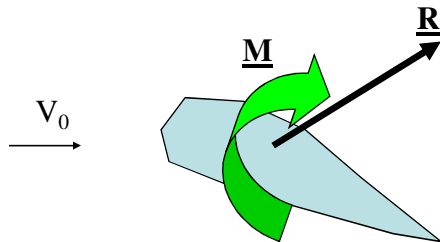
- Pressure Taps Located Around Airfoil Surface
- Provide $P(\underline{x})$ Data
- Integrate This Data Over Airfoil Surface to Find Net Force Vector & Moment....

Aerodynamic Forces in Airfoil



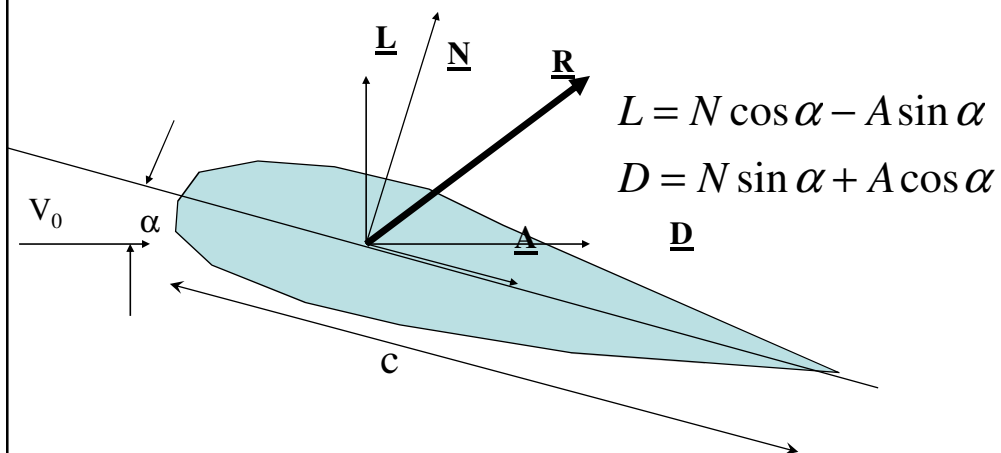
- Pressure Distribution on Body Surface Given as $P(s)$
 - Shear Stress on Body Surface given as $\tau(s)$
 - P acts normal to surface
 τ acts tangential to surface
- Both have Force/Area Units

Integrating P and τ Distributions Gives Force & Moments on Airfoil



- Total Force, \underline{R} , Can Be Resolved into Lift Force, \underline{L} and Drag Force \underline{D}
 - \underline{L} acts perpendicular to V_0
 - \underline{D} acts parallel to V_0

Lift & Drag Forces



$$L = N \cos \alpha - A \sin \alpha$$

$$D = N \sin \alpha + A \cos \alpha$$

\underline{N} , \underline{A} - Normal, Axial components w/r/t chord

\underline{D} , \underline{L} - Axial, Normal components w/r/t free stream V_0

Integrate Pressure Over Surface to Find Net Force:

Dimensionless Pressure Coefficient:

$$C_p = \frac{p - p_{ref}}{\frac{1}{2}\rho U^2}$$

Normal Force Coefficient:

$$C_n = \frac{N}{\frac{1}{2}\rho V_0^2 A_{span}} \approx \frac{1}{c} \int_0^c (C_{p_L} - C_{p_U}) dx$$

Neglecting Skin Shear Stress Effects

Determine Lift Coefficient from Normal Force Coefficient

- Use the Geometry to Find

$$L = N \cos \alpha - A \sin \alpha$$

- Usually $A \ll N$, Thus Can Approximate

$$C_L \approx C_N \cos \alpha$$

- Note That the Assumption $A \ll N$ Implies Drag Force is Small (I.e. we are taking $C_d \sim 0$).

Determine Pitching Moment Coefficient from Pressure Coefficient Distribution

- Use the Geometry to Find

$$C_{m_{\text{ref}}} = \frac{1}{c^2} \int_0^c (C_{pU} - C_{pL})(x - x_{\text{ref}}) dx$$

- Conventional X_{ref} is Quarter-chord Location

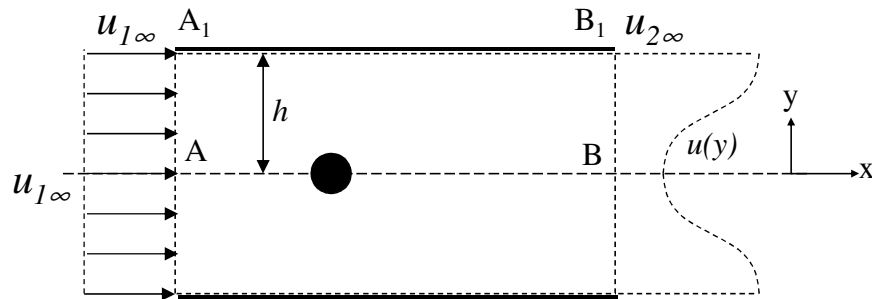
- Center-of-Pressure Location Is Then Given as

$$\frac{X_{\text{cp}}}{c} = -\frac{C_{M_{LE}}}{C_N}$$

Part 2

- Drag from Momentum Loss Measured in Wake with Pressure Array

Drag Coefficient



● incompressible

Drag Coefficient

Mass Conservation

Cross Section: (Rate of Flow)

$$AB = 0$$

$$AA_1 = \rho b \int_0^h u_{1\infty} dy = \rho b h u_{1\infty}$$

$$BB_1 = -\rho b \int_0^h u dy$$

$$A_1B_1 = -\rho b \int_0^h (u_{1\infty} - u) dy$$

Drag Coefficient

Equation of Motion – steady Flow:

$$\iiint [\nabla \cdot (\rho \vec{w} \vec{w})] dV = Drag$$

Reynolds Transport Theorem

$$\iiint \vec{\nabla} \cdot \vec{F} dV = \iint \vec{F} \cdot \vec{n} dA$$

If static pressure on AA₁, BB₁ are same

Drag Coefficient

Equation of Motion

Cross Section	$\int \rho \vec{w} \vec{w} \cdot \vec{n} dA$
AB	0
AA ₁	$\rho b h u_{1\infty}^2$
BB ₁	$-\rho b \int_0^h u^2 dy$
A ₁ B ₁	$-\rho b \int_0^h u_{1\infty} (u_{1\infty} - u) dy$
<hr style="width: 50%; margin: 0 auto;"/>	
$Drag = 2\rho b \int_0^h u (u_{1\infty} - u) dy$	
$= 2\rho b u_{1\infty}^2 \int_0^h \frac{u}{u_{1\infty}} \left[1 - \frac{u}{u_{1\infty}} \right] dy$	

Drag Coefficient

Drag on Cylinder:

Per unit length ($b = 1$)

$$Drag = 2\rho b u_{1\infty}^2 \int_0^h \frac{u}{u_{1\infty}} \left[1 - \frac{u}{u_{1\infty}} \right] dy$$

The Drag Coefficient C_D

- Drag Coefficient is computed from drag, D :

$$C_d = \frac{D}{\frac{1}{2} \rho V_0^2 A_{span}}$$

- Use Previous Expression for Drag to Find C_d From Momentum Analysis:

$$C_d = \frac{Y_w}{c} - \frac{1}{q_{\infty} c} \int_{-\frac{Y_w}{2}}^{\frac{Y_w}{2}} q \, dy$$

where
 $q = \frac{1}{2} \rho V^2(y)$
 $Y_w \sim$ Wakefield array width

Wakefield Procedure

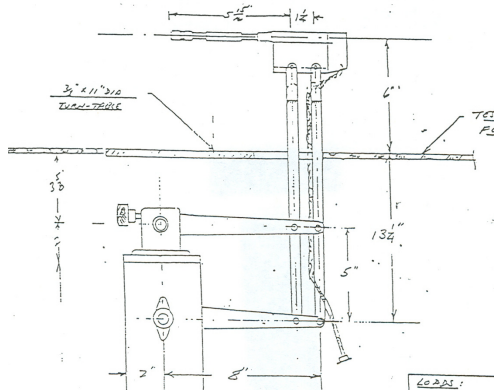
- Operate Tunnel at Desired Flowspeed & Airfoil Angle-of-Attack
- Make Sure Wakefield Array Covers Entire Wake
- Gather $q(y)$ data
- Use Theory to Find Drag Force, Coefficient

Part 3

- Direct Measurement with Mechanical force Balance

Mechanical Force Balance

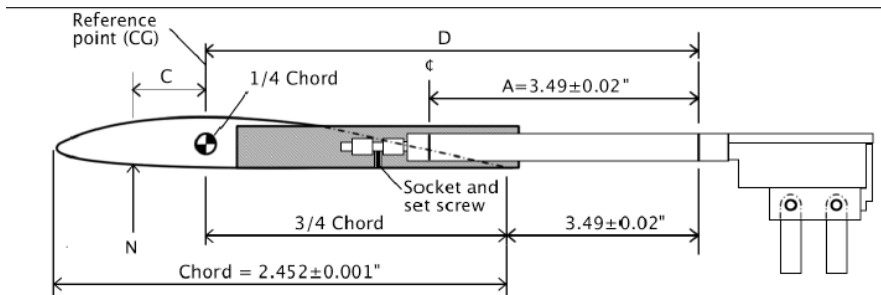
Force Balance Mechanism



- Mount Airfoil on Small “Sting”, or cylinder holder
- Sting Attaches to Load Frame
- Strain Gauges Used to Measure Forces & Moments on Sting Assembly

Mechanical Force Balance

Airfoil & Sting Detail



Airfoil Span (overall length of airfoil) = 9.8125 ± 0.0625 "
 c - Balance center
 (Marked on wing section)

Mechanical Force Balance

- The lift, drag, and pitching forces on the airfoil can be calculated from a force balance measurements of the axial force A' , normal force N' , and pitching moment P' relative to the sting support on the balance.
- The values of A' , N' , and P' are measured from strain gauge bridges on the force balance and are not independent.
- Compensate for this interaction between the measured values with matrix:

$$\begin{aligned}N &= N'*.9504-A'*.0082-P'*.0161 \\A &= N'*.0608+A'*.5912 \\P &= -N'*.1336+A'*.0119+P'*.182\end{aligned}$$

References

1. John D. Anderson, "Fundamentals of Aerodynamics", 2nd Ed., pp. 195-200 and pp. 228-236, McGraw Hill 1991.